



Technische Universität München

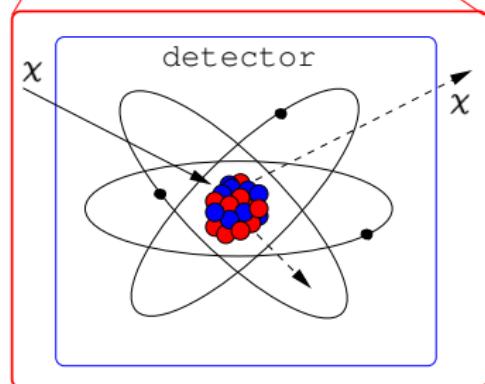
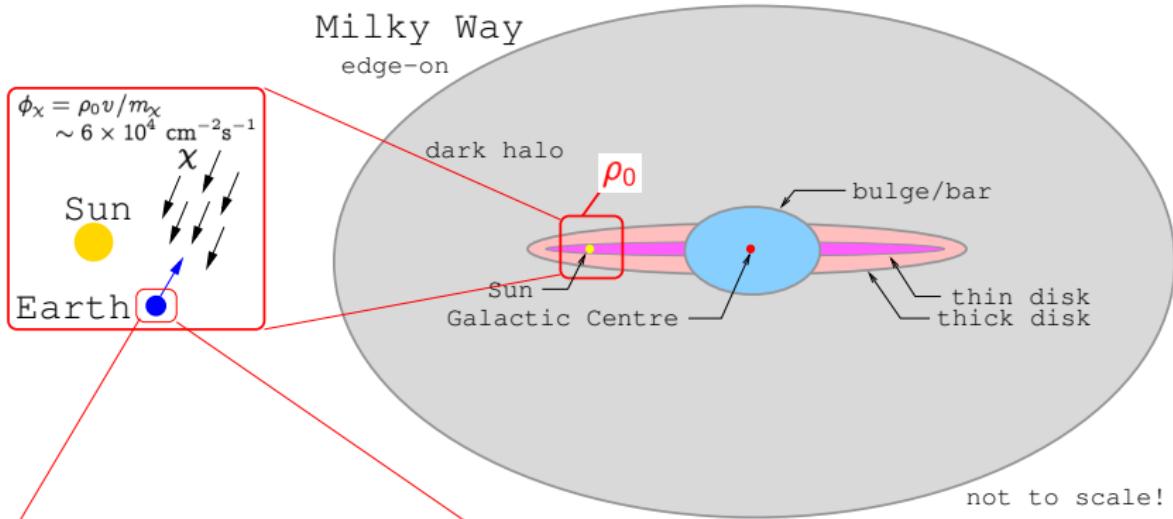


ASTROPHYSICAL UNCERTAINTIES IN DIRECT DARK MATTER SEARCHES

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Physik-Department T30d, Technische Universität München

1. DIRECT DARK MATTER SEARCHES



driving idea: detect WIMP scattering off nuclei

$$\frac{dR}{dE_R} = \frac{1}{m_N} \int_{v_{min}}^{\infty} d^3 \vec{v} \frac{\rho_0 v}{m_\chi} f(\vec{v} + \vec{v}_e) \frac{d\sigma_{\chi-N}}{dE_R}$$

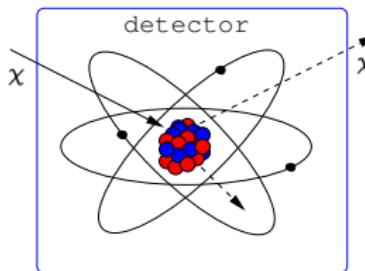
astrophysics

nuclear/particle physics

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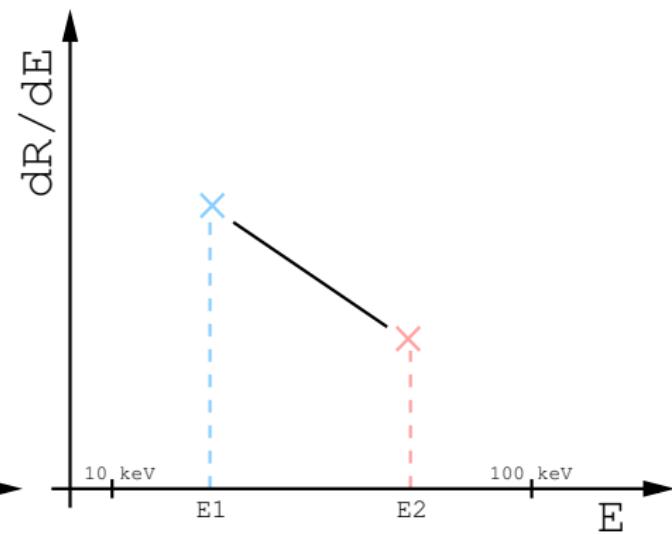
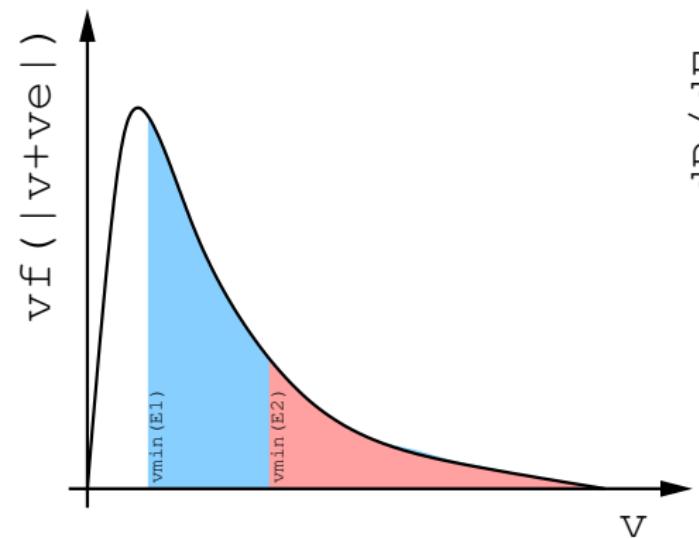
WIMP signatures

1. exponential recoil spectrum



$$v_{min} = \sqrt{\frac{m_N E_R}{2\mu_N^2}}$$

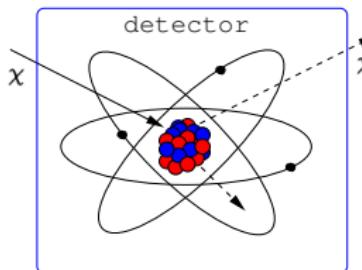
$$f(w) \propto \exp(-w^2/2\sigma^2)$$



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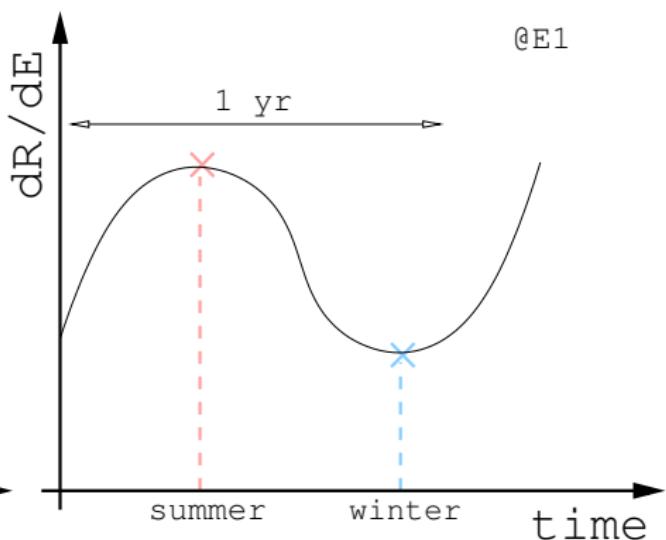
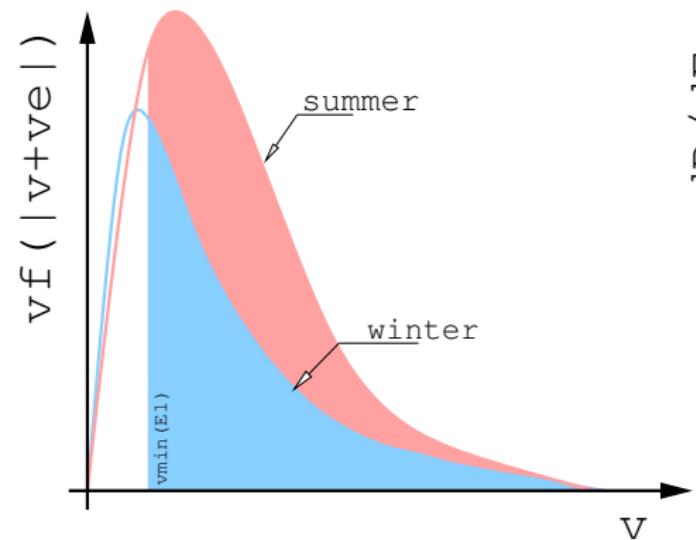
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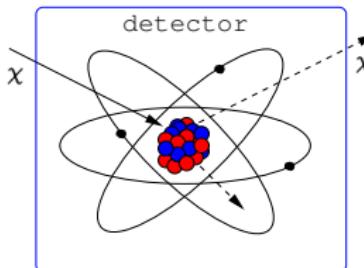
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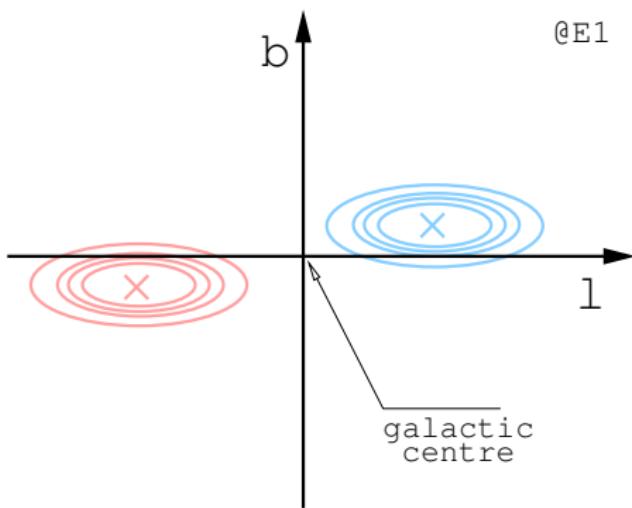
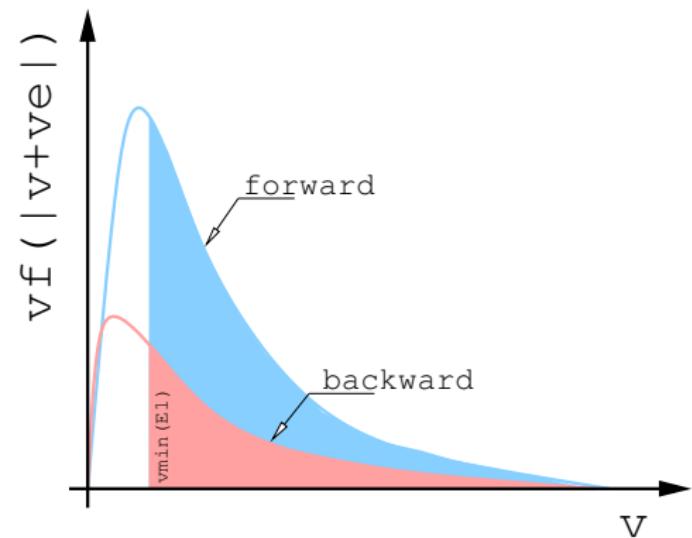
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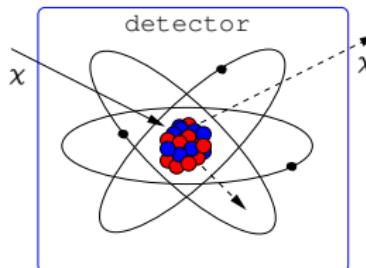
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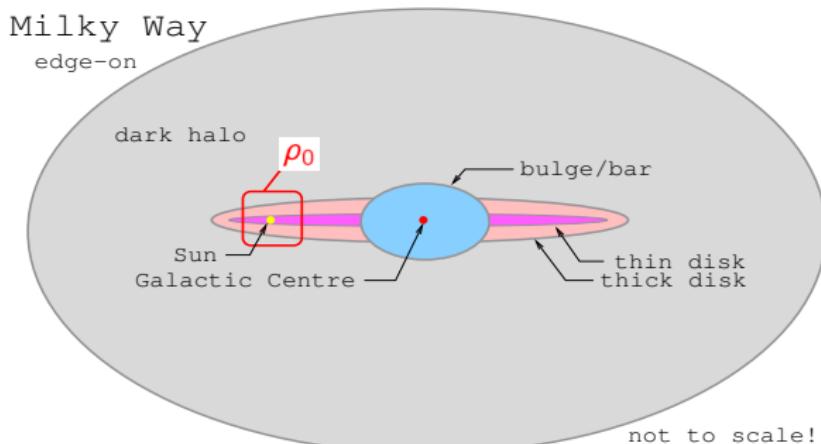
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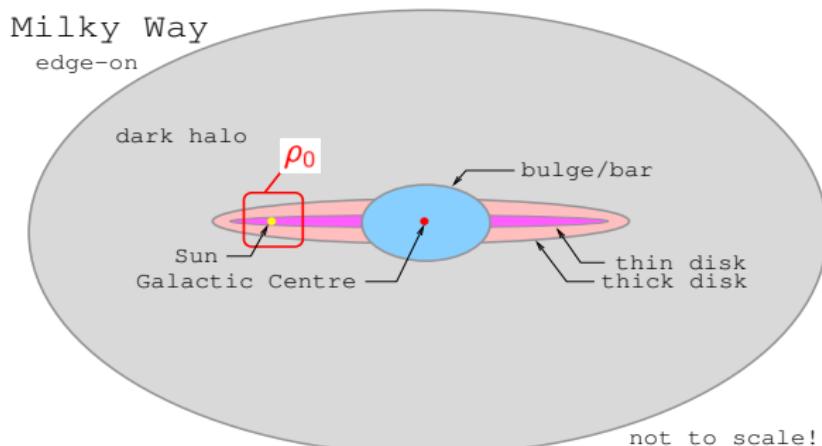
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assuming we know well the dark matter distribution... but do we?

2. MILKY WAY MASS MODELLING

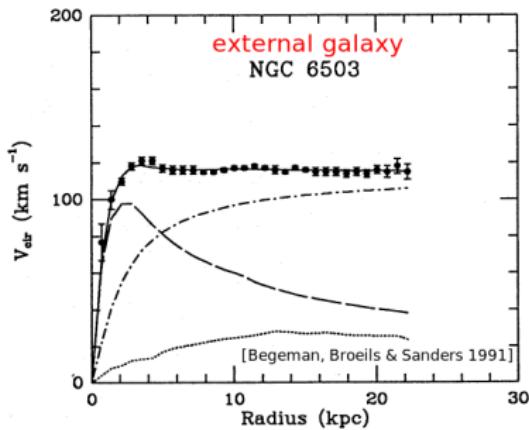
bulge(+bar) $\lesssim 3$ kpc
disk $\lesssim 10$ kpc
dark halo $\lesssim 200$ kpc $\rho_{DM} \propto \rho_0 r^{-\alpha} (1 + r/r_s)^{-3+\alpha}$
+gas...



how can we constrain the parameters of a MW mass model?

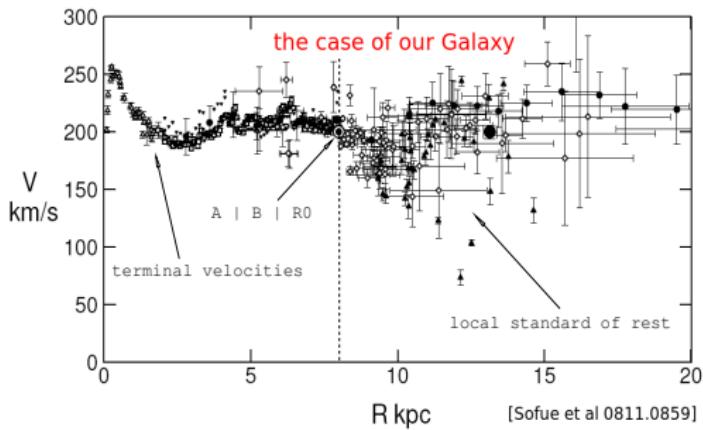
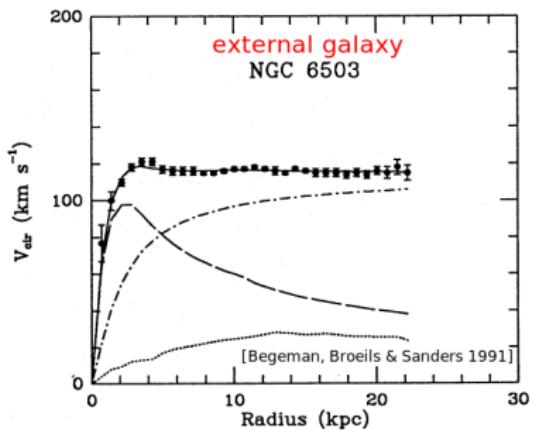
2. MILKY WAY MASS MODELLING

rotation curve traces total potential



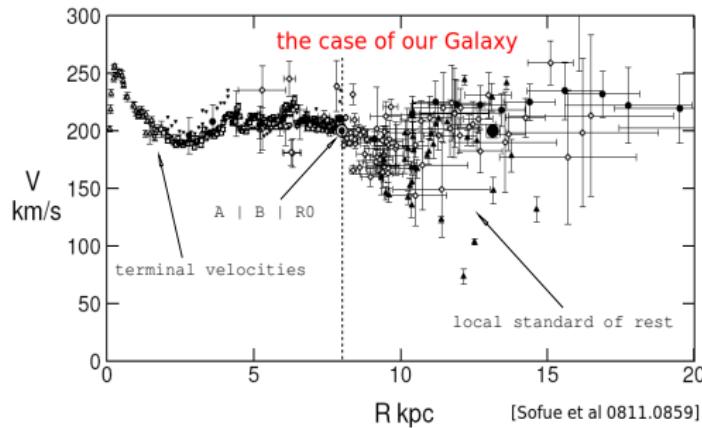
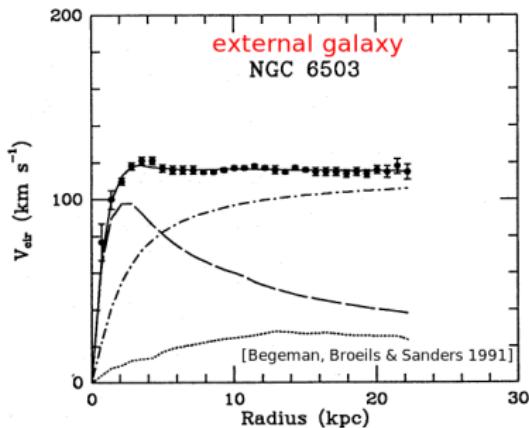
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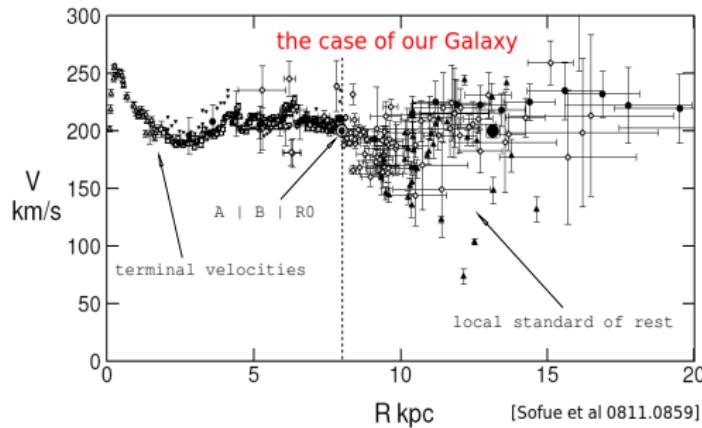
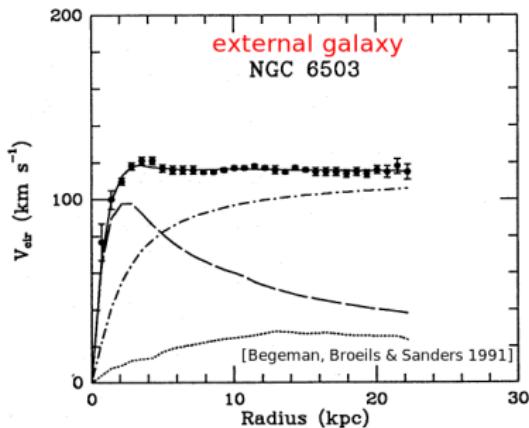
satellite dynamics traces total mass enclosed at $R \sim \mathcal{O}(100)$ kpc

star counts and dynamics

- .. σ_v in tracers: traces total potential at $R \sim \mathcal{O}(50)$ kpc
- .. Oort's limit: traces local total surface density
- .. local luminosity: traces local visible surface density

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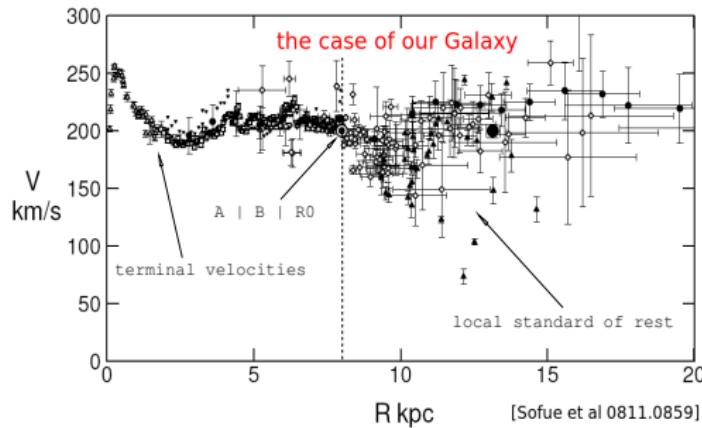
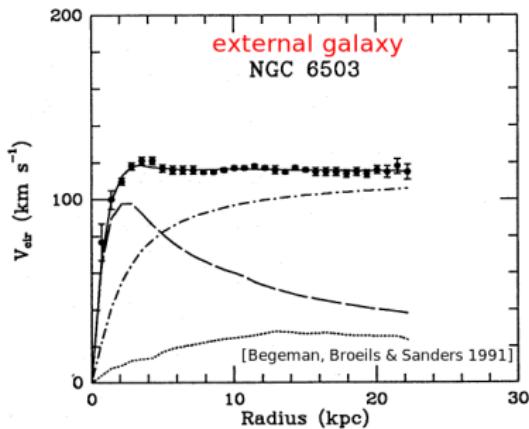
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gravitational microlensing

traces the density of lenses along l.o.s.

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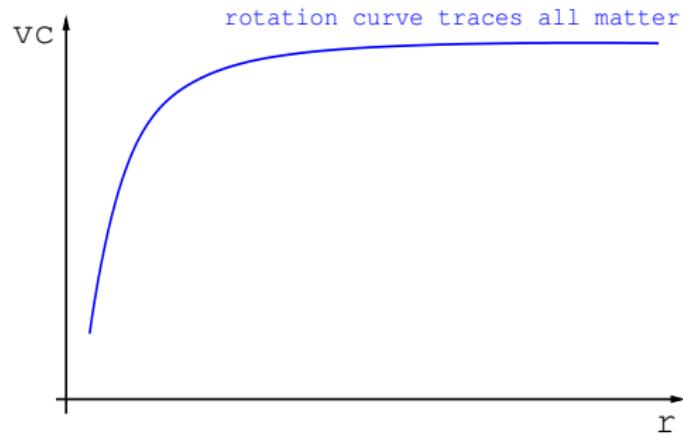
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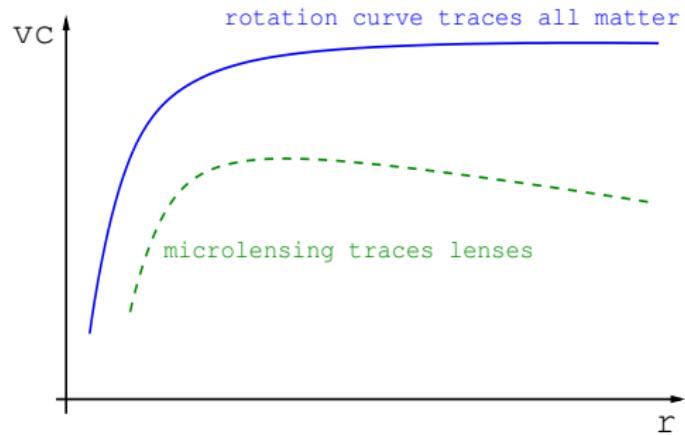
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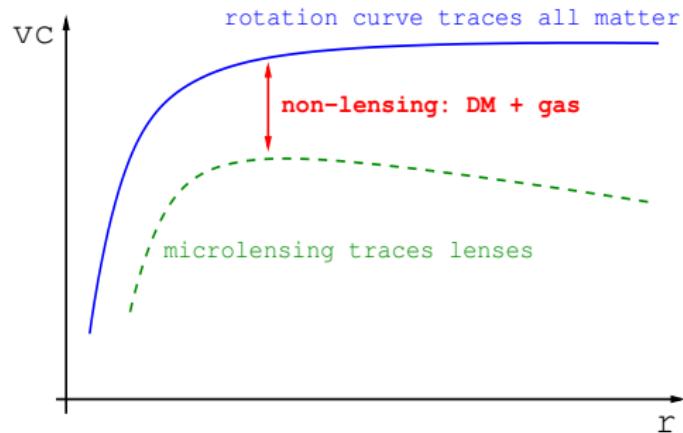
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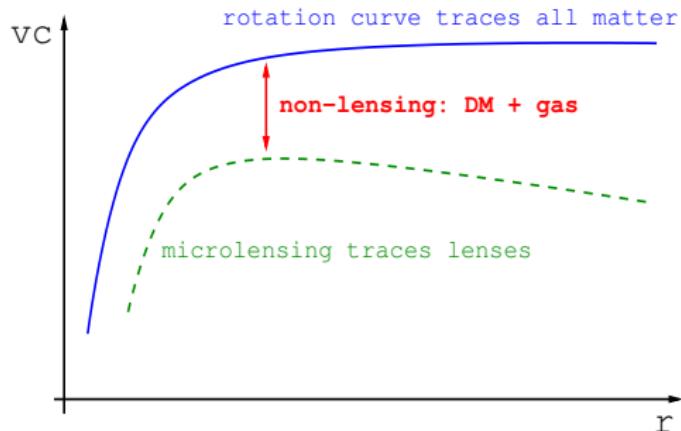


2. MICROLENSING + DYNAMICS: THE IDEA



bottomline rotation curve + microlensing constrain DM profile

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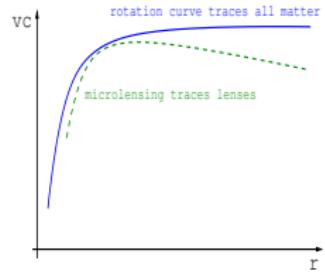
bottomline rotation curve + microlensing constrain DM profile

Binney & Evans 2001

conclude that cuspy profiles are inconsistent (!!)

but:

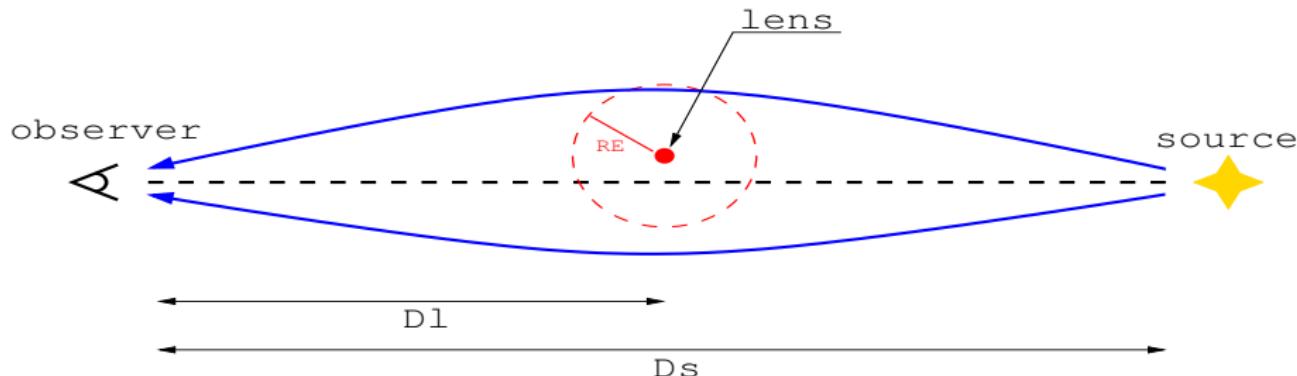
- .. new microlensing data released
- .. poor v_c treatment
- .. simplified MW mass modelling



2. GRAVITATIONAL MICROLENSING: BASICS

microlensing is a direct consequence of GR

[Paczynski '86]



$$R_E^2 = \frac{4GM_l}{c^2} D_l \left(1 - \frac{D_l}{D_s}\right)$$

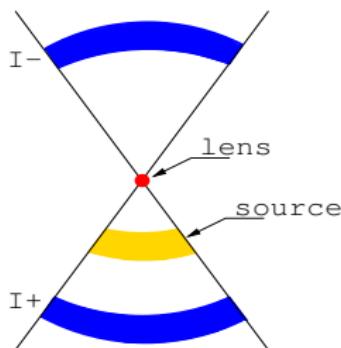
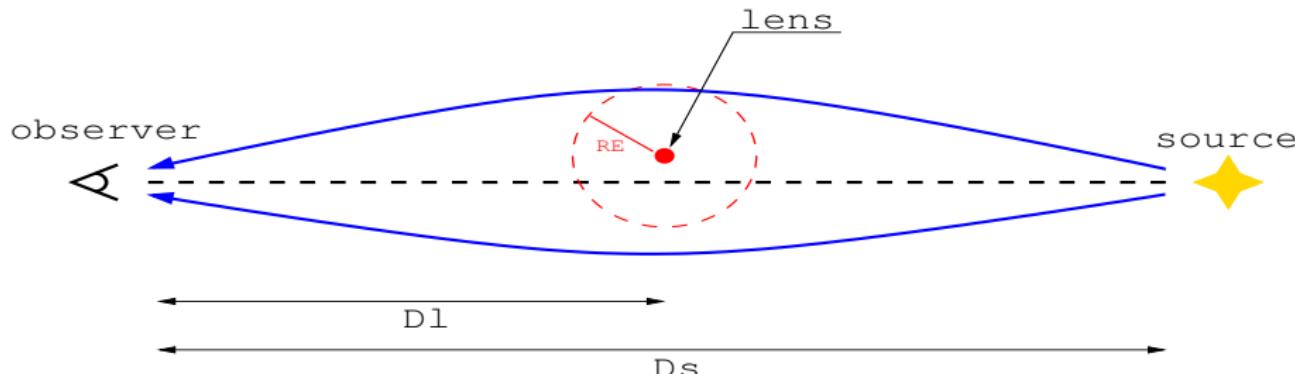
unresolved images $A(t) = \frac{u^2+2}{u\sqrt{u^2+4}}$

$$M_l \sim [10^{-6}, 10^2] M_\odot; \quad t_E \sim \text{hr} - \text{days}$$

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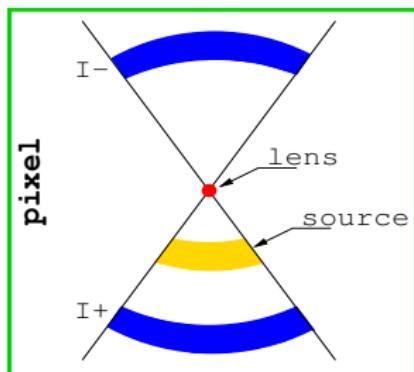
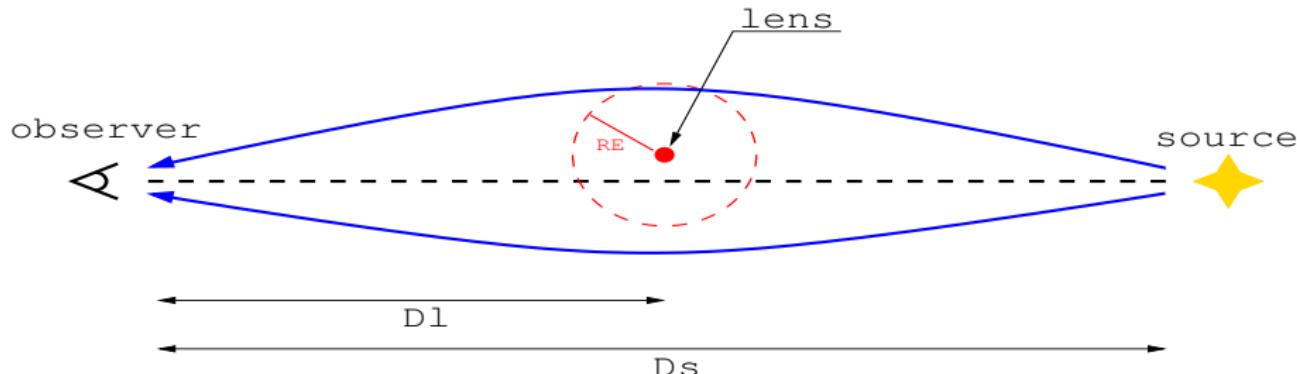
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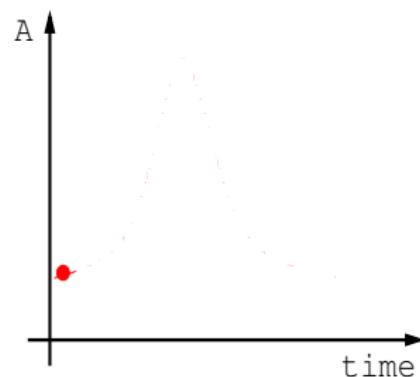
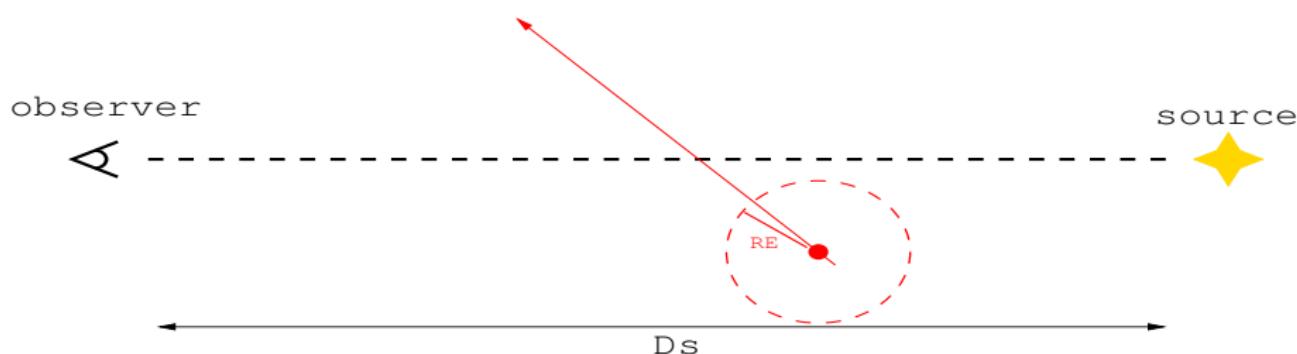
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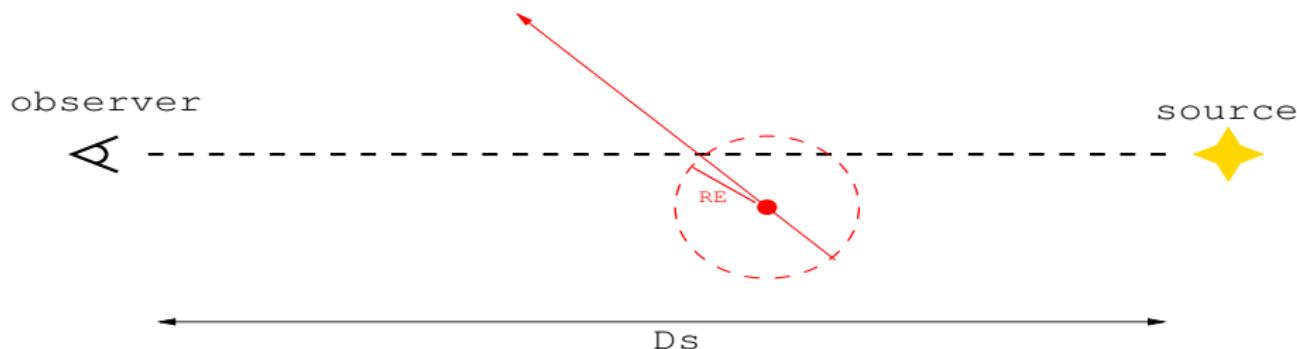
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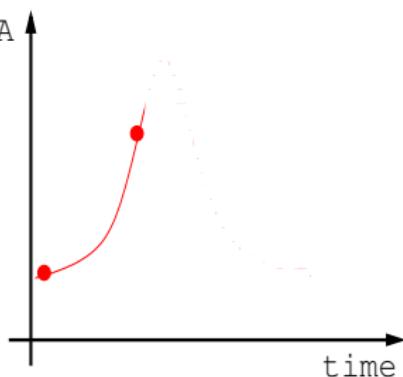
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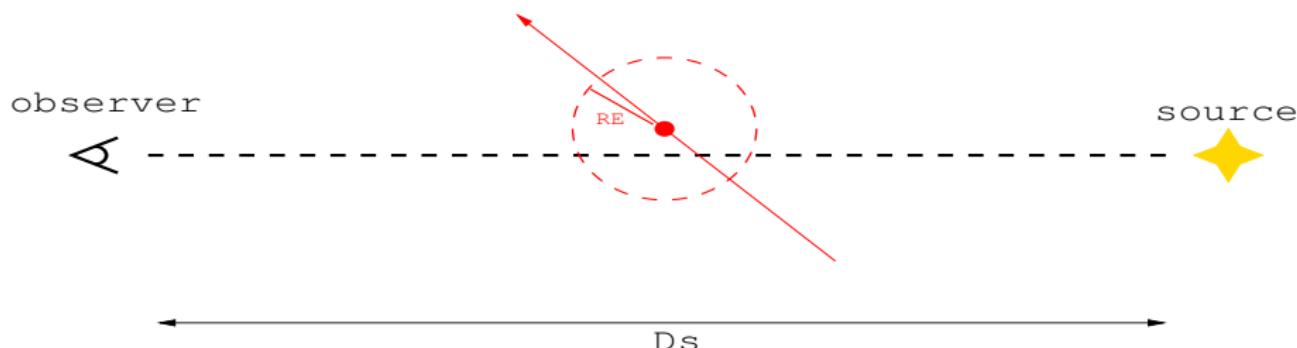
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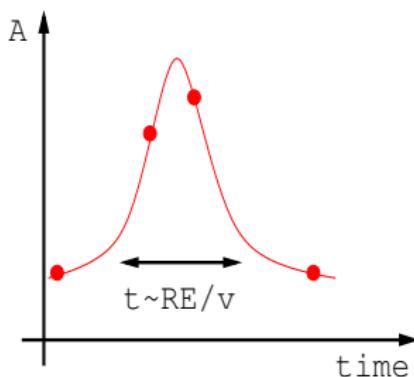
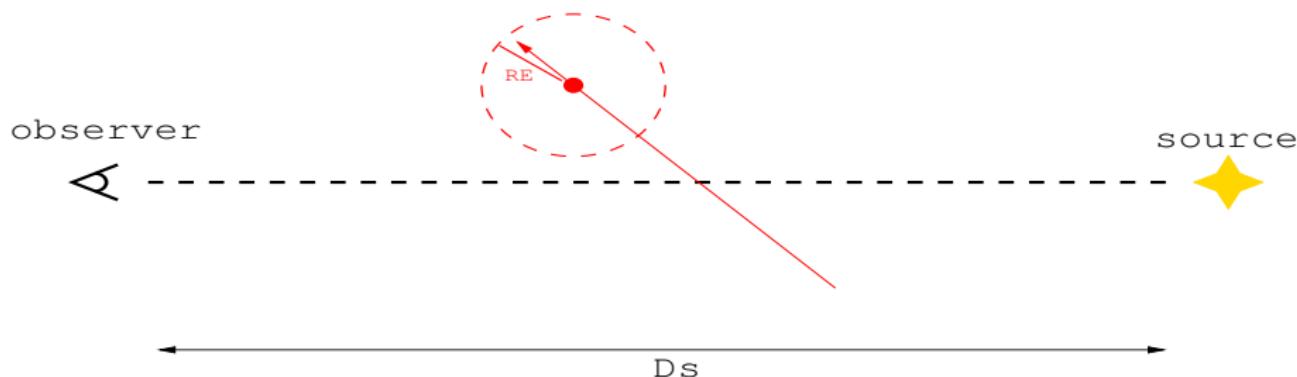
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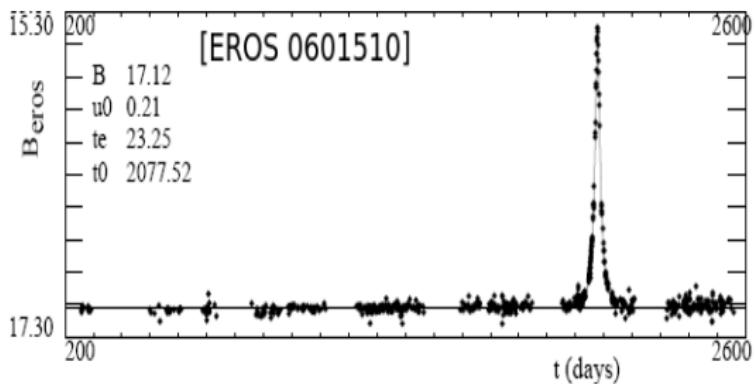
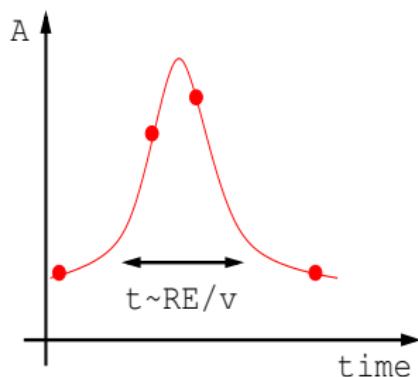
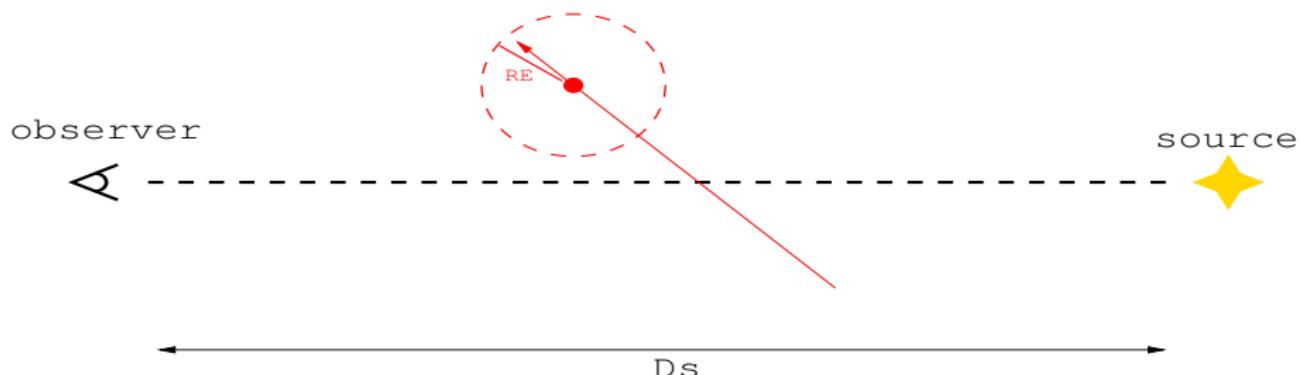
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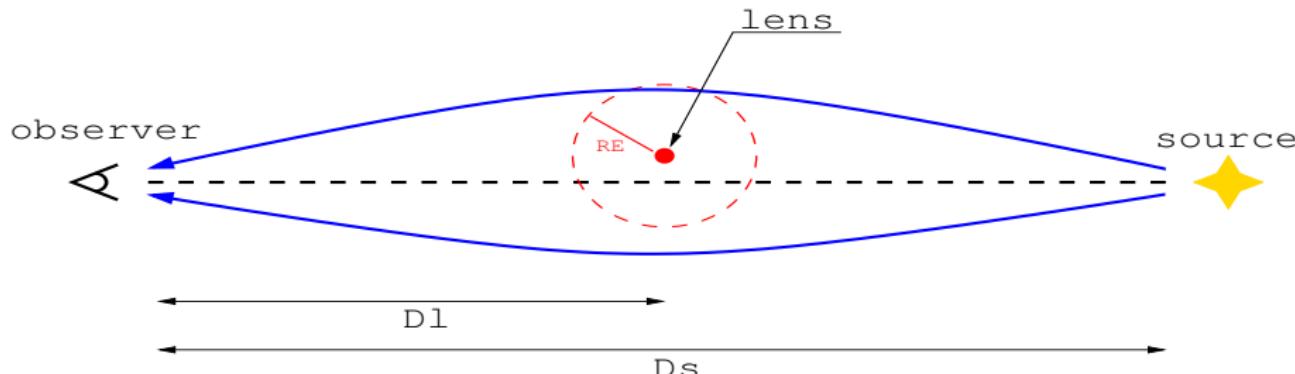
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optical depth probability for observing a microlensing event

$$\tau = \int_0^{D_s} dD_l \int dM_l \left(\pi R_E^2 \right) \times \left(\frac{d^2 N_l}{dV dM_l} \right) = \frac{4\pi G}{c^2} \int_0^{D_s} dD_l \rho_l D_l \left(1 - \frac{D_l}{D_s} \right)$$

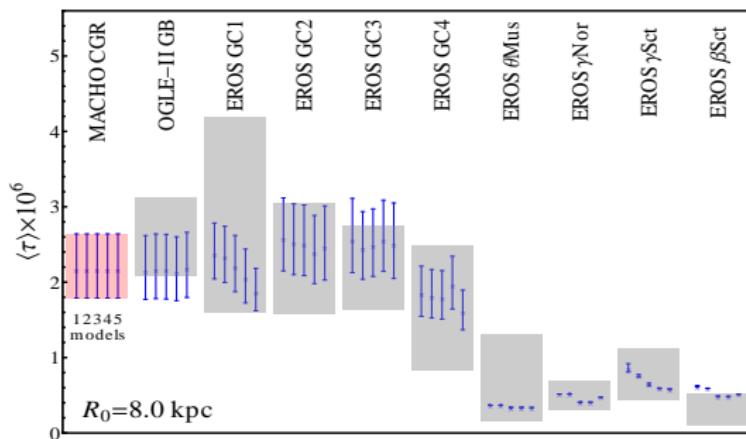
just depends on ρ_l , not on M_l !

2. MICROLENSING + DYNAMICS: METHODOLOGY

1. fix $\rho_{0,b}$ to match MACHO '05 $\langle \tau \rangle = 2.17^{+0.47}_{-0.38} \times 10^{-6}$

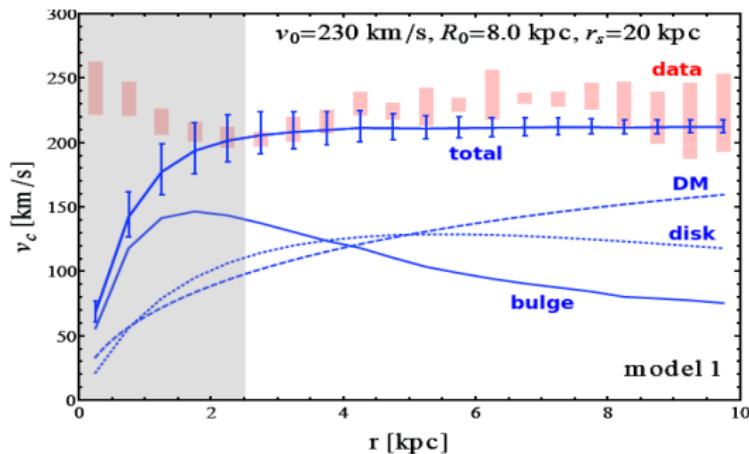
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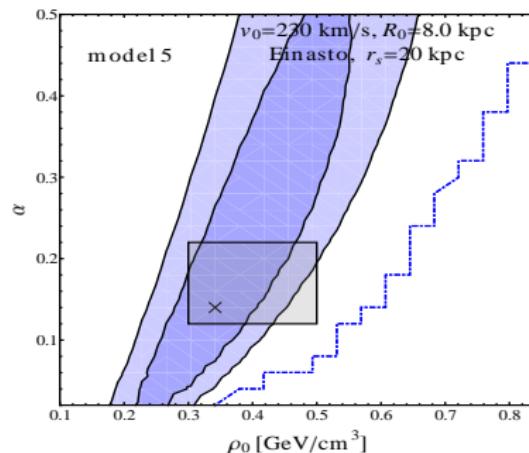
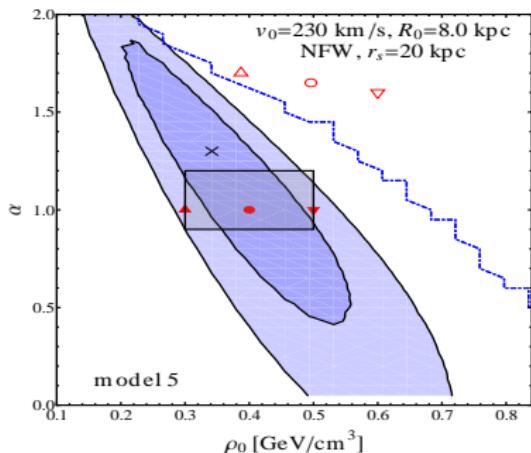
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NFW with $(\rho_0, \alpha) = (0.4 \text{ GeV/cm}^3, 1.0)$

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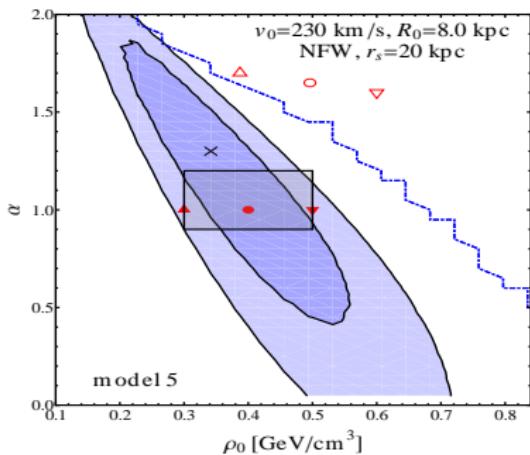
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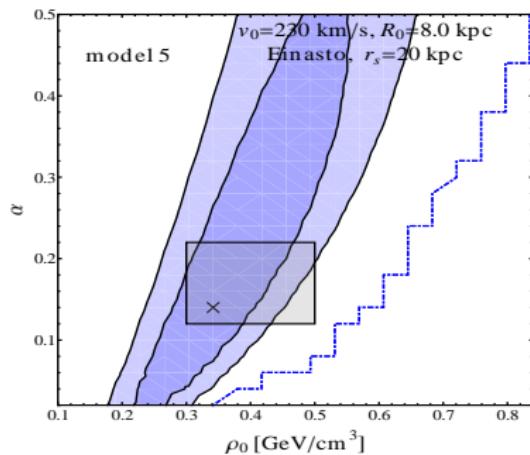
excellent agreement with findings of numerical simulations

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$$\rho_0 = 0.20 - 0.56 \text{ GeV/cm}^3 \text{ (NFW)}$$

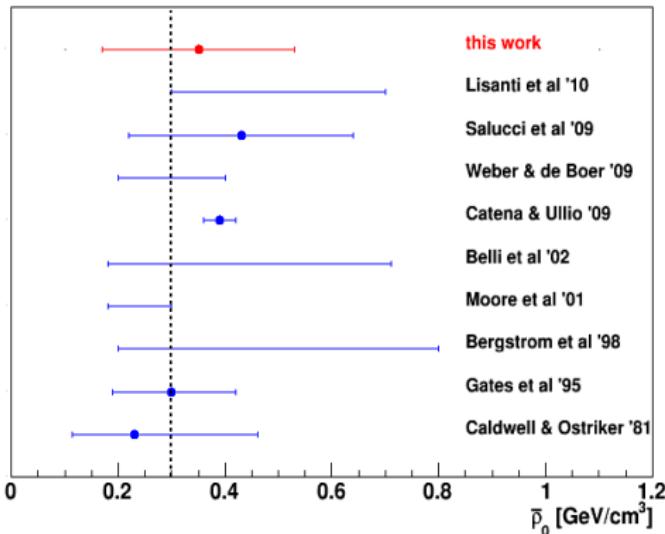


$$\rho_0 = 0.22 - 0.55 \text{ GeV/cm}^3 \text{ (Ein)}$$

2. MICROLENSING + DYNAMICS: SUMMARY

NFW: $\rho_0 = 0.20 - 0.56 \text{ GeV/cm}^3$ $\alpha = 0.4 - 1.8$

[Iocco, MP, Bertone & Jetzer, arXiv:1107.5810]



bottomline

- .. not competitive with other measurements e.g. Catena & Ullio '09
- .. but complementary technique
- .. huge potential: constrain local density, profile slope and shape

3. IMPACT ON DIRECT SEARCHES

spin-independent scattering rate

$$\frac{dR}{dE_R} = \frac{\rho_0 \sigma_{SI}^p}{2m_\chi \mu_{p\chi}^2} \times \underbrace{\mathbf{A}^2 F^2(E_R, \mathbf{A})}_{\text{nuclear physics}} \times \underbrace{\mathcal{F}(v_{min}(E_R, \mathbf{A}, m_\chi))}_{\text{astrophysics}}$$

$$\mathcal{F} \equiv \int_{v > v_{min}} d^3 \vec{v} \frac{f(\vec{v} + \vec{v}_e)}{v} \quad v_{min}(E_R) = \frac{1}{\sqrt{2m_N E_R}} \left(\frac{m_N E_R}{\mu_N} + \delta \right)$$

standard halo model

$$\rho_0 = 0.3 \text{ GeV/cm}^3$$

$$f(w) \propto \begin{cases} \exp(-w^2/v_0^2) & \text{for } w \leq v_{esc} \\ 0 & \text{for } w > v_{esc} \end{cases}$$

$$v_0 \equiv 2\sqrt{\sigma_{1d}} = v_c^0 \simeq 220 \text{ km/s}$$

$$v_{esc} \simeq 600 \text{ km/s}$$

good starting point but huge uncertainties on the parameters ρ_0 , v_c^0 , v_{esc}

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spin-independent scattering rate

$$\frac{dR}{dE_R} = \frac{\rho_0 \sigma_{SI}^p}{2m_\chi \mu_{p\chi}^2} \times \underbrace{\mathbf{A}^2 F^2(E_R, \mathbf{A})}_{\text{nuclear physics}} \times \underbrace{\mathcal{F}(v_{min}(E_R, \mathbf{A}, m_\chi))}_{\text{astrophysics}}$$

$$\mathcal{F} \equiv \int_{v > v_{min}} d^3 \vec{v} \frac{f(\vec{v} + \vec{v}_e)}{v} \quad v_{min}(E_R) = \frac{1}{\sqrt{2m_N E_R}} \left(\frac{m_N E_R}{\mu_N} + \delta \right)$$

our approach

$$f(w) \propto \begin{cases} \left[\exp \left(\frac{v_{esc}^2 - w^2}{kv_0^2} \right) - 1 \right]^k & \text{for } w \leq v_{esc} \\ 0 & \text{for } w > v_{esc} \end{cases} \quad (\text{see Lisanti et al 2010})$$

$$v_e \sim v_c^0 \quad v_0 = v_c^0$$

fiducial: $\rho_0 = 0.4 \text{ GeV/cm}^3, k = 1, v_{esc} = 544 \text{ km/s}, v_0 = 230 \text{ km/s}$

crucial point: huge uncertainties on $\rho_0, v_c^0, v_{esc}, k$

3. IMPACT ON DIRECT SEARCHES

local DM density

$$\rho_0 = 0.4 \pm 0.1 \text{ GeV/cm}^3 \quad (1\sigma)$$

(Catena & Ullio + systematics)

circular velocity

$$v_0 = v_c^0 = 230 \pm 30 \text{ km/s} \quad (1\sigma)$$

(perhaps optimistic!)

escape velocity

$$v_{esc} = 544 \pm 33 \text{ km/s} \quad (1\sigma)$$

(Smith et al 2006, RAVE survey)

shape parameter

$$k = 0.5 - 3.5 \quad (\text{flat})$$

(Lisanti et al 2010 \oplus k=1)

key question: how do these uncertainties impact direct searches?

[MP, Baudis, Bertone, de Austri, Strigari & Trotta '11]

3. IMPACT ON DIRECT SEARCHES

fast forward to ~2020

MP, Baudis, Bertone, de Austri, Strigari & Trotta, PRD 2011

- .. use next generation of experiments Xe, Ge, Ar
- .. study the complementarity of targets
- .. include astrophysical uncertainties

3. IMPACT ON DIRECT SEARCHES

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upcoming experimental capabilities

noble liquids

DARWIN $\sigma_{SI}^p < 10^{-47} \text{ cm}^2$ (2016)

cryogenic

EURECA $\sigma_{SI}^p > 10^{-46} \text{ cm}^2$ (2018)

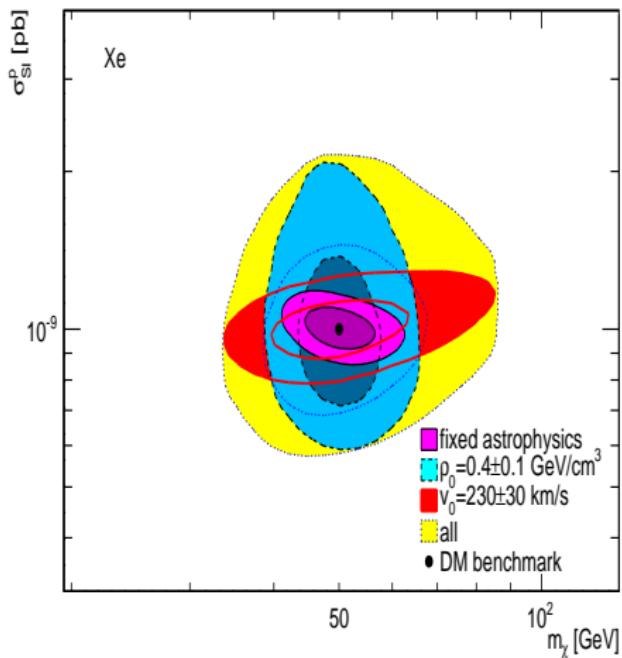
10 yr from now

target	ϵ [ton \times yr]	η_{cut}	A_{NR}	ϵ_{eff}	[ton \times yr]	E_{thr} [keV]	$\sigma(E)$ [keV]	background events/ ϵ_{eff}
Xe	5.0	0.8	0.5	2.00	10	Eq. (7)		< 1
Ge	3.0	0.8	0.9	2.16	10	Eq. (6)		< 1
Ar	10.0	0.8	0.8	6.40	30	Eq. (8)		< 1

[MP, Baudis, Bertone, de Austri, Strigari & Trotta '11]

3. IMPACT ON DIRECT SEARCHES

varying astrophysics



$$\begin{aligned}\rho_0 &= 0.4 \pm 0.1 \text{ GeV/cm}^3 \\ v_0 &= 230 \pm 30 \text{ km/s} \\ v_{esc} &= 544 \pm 33 \text{ km/s} \\ k &= 0.5 - 3.5\end{aligned}$$

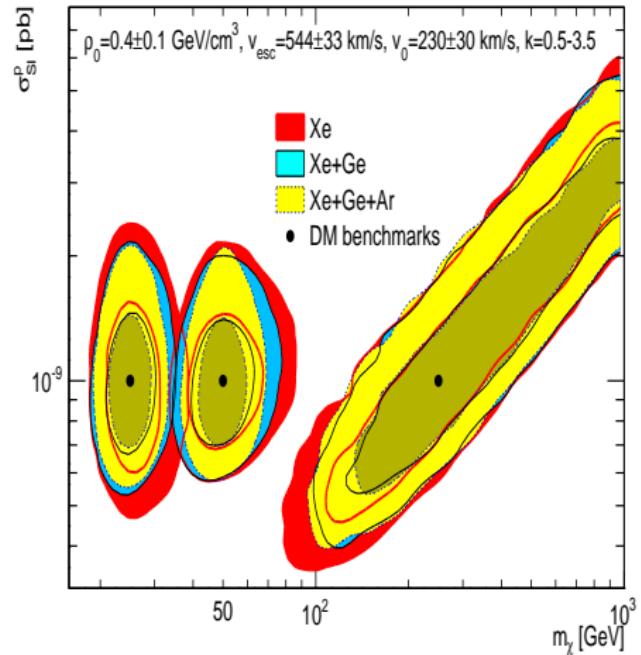
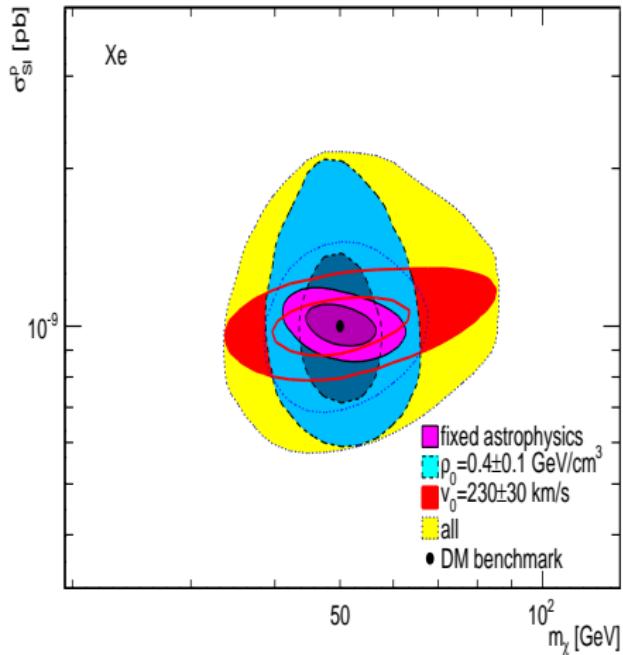
most relevant are ρ_0 and v_0 :

ρ_0 : deg. with σ_{SI}^p , $\frac{dR}{dE_R} \propto \rho_0 \sigma_{SI}^p$

v_0 : deg. with m_χ , $\frac{dR}{dE_R} \propto \frac{1}{m_\chi v_0}$

3. IMPACT ON DIRECT SEARCHES

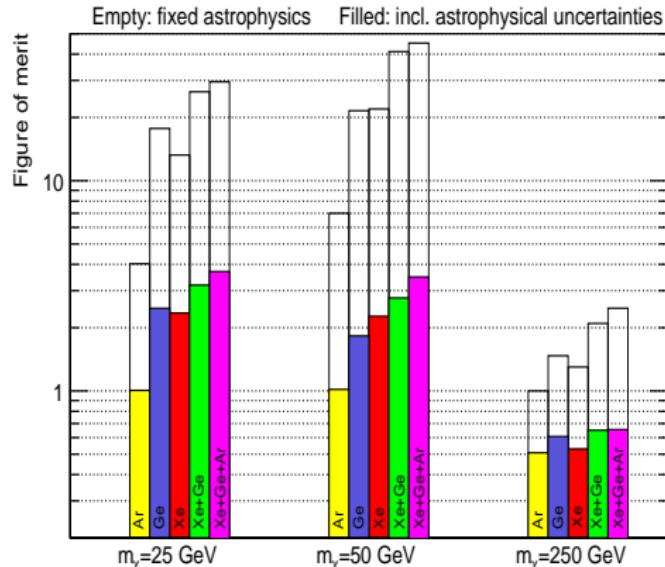
varying astrophysics



[MP, Baudis, Bertone, de Austri, Strigari & Trotta '11]

3. TARGET COMPLEMENTARITY

figure of merit: $(95\% \text{ contour area in the plane } \log_{10} m_\chi - \log_{10} \sigma_{SI}^p)^{-1}$

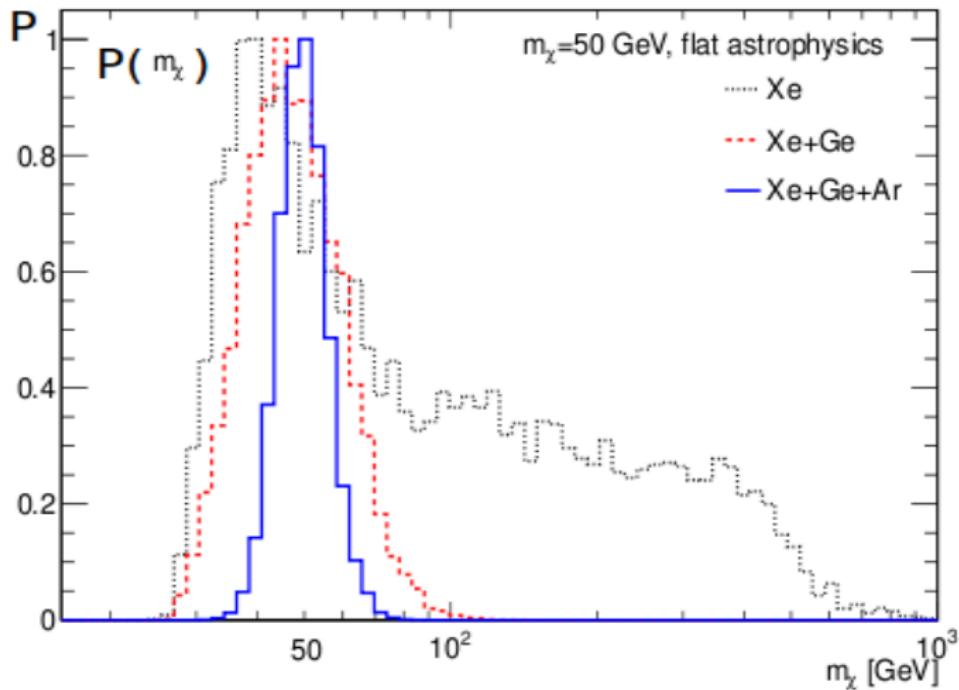


- .. astrophysical uncertainties reduce constraining power
- .. Ge best at $m_\chi = 25, 250$ GeV; Xe best at $m_\chi = 50$ GeV
- .. astrophysical uncertainties affect target complementarity in a non-trivial way

3. TARGET COMPLEMENTARITY

let us be conservative:

what can be robustly measured irrespective of astrophysics?



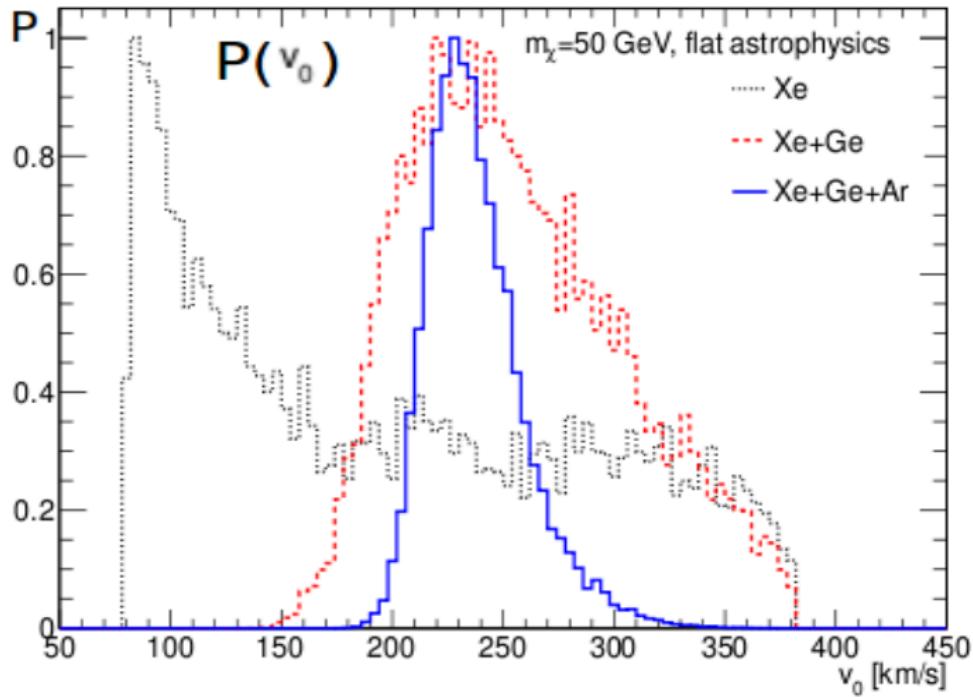
.. wimp mass m_χ : within 10's GeV

[MP, Baudis, Bertone, de Austri, Strigari & Trotta '11]

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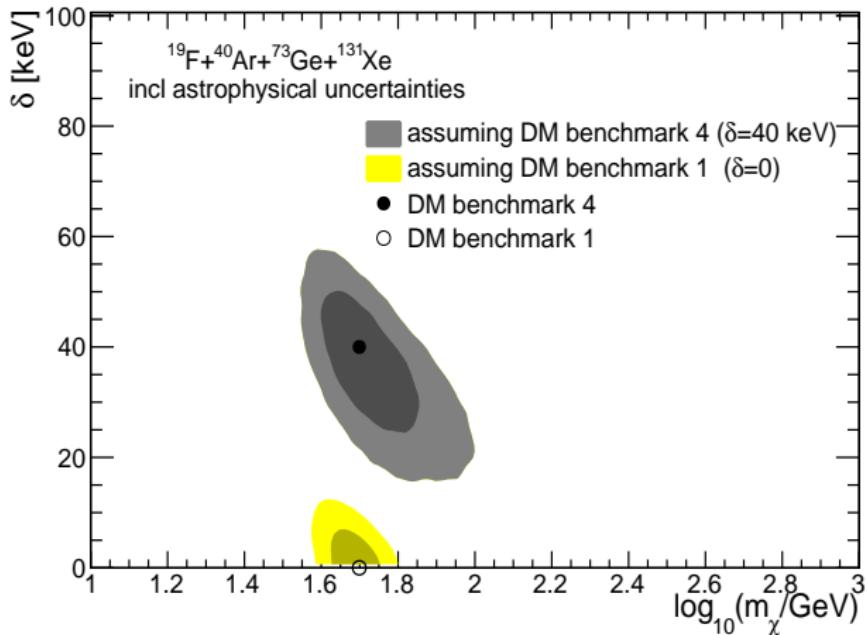
.. local circular velocity v_0 : within 10's km/s

[MP, Baudis, Bertone, de Austri, Strigari & Trotta '11]

3. TARGET COMPLEMENTARITY

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.. inelastic parameter δ : within 10's keV

4. TO WRAP UP...

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- .. microlensing + dynamical: powerful, complementary technique
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future for dark matter searches?

complementarity direct+indirect+collider searches
accurate description of dark matter distribution